



Algorithms: Design
and Analysis, Part II

NP-Completeness

The P vs. NP
Question

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Question: Is $P = NP$?

polynomial time solvable

can verify correctness of a solution in polynomial time

Widely conjectured: $P \neq NP$. [Though see Gödel '56]

But: Has not been proved. [Worth \$1 million from Clay Institute]

Reasons to believe:

- (1) (psychological) if $P=NP$, someone would have proved it by now
- (2) (philosophical) if $P=NP$, then finding a proof always as easy as verifying one
- (3) (mathematical) ??

What's In A Name

FAQ: What does “NP” stand for?

~~“not polynomial”~~

Answer: “Nondeterministic polynomial”

[Modern, mathematically equivalent definition via efficient verification of purported solutions]

Historical reference: Knuth, “A Terminological Proposal”, 1974.

Passed over:

