



Design and Analysis
of Algorithms I

Master Method

Intuition for the 3 Cases

How To Think About (*)

Our upper bound on the work at level j :

$$cn^d \times \left(\frac{a}{b^d}\right)^j$$

Interpretation

a = rate of subproblem proliferation (RSP)

b^d = rate of work shrinkage (RWS)

(per subproblem)

Which of the following statements are true?
(Check all that apply.)

-  If $RSP < RWS$, then the amount of work is decreasing with the recursion level j .
-  If $RSP > RWS$, then the amount of work is increasing with the recursion level j .
- No conclusions can be drawn about how the amount of work varies with the recursion level j unless RSP and RWS are equal.
-  If RSP and RWS are equal, then the amount of work is the same at every recursion level j .

Intuition for the 3 Cases

Upper bound for level j : $cn^d \times \left(\frac{a}{b^d}\right)^j$

1. $RSP = RWS \Rightarrow$ Same amount of work each level (like Merge Sort) [expect $O(n^d \log(n))$]
2. $RSP < RWS \Rightarrow$ less work each level \Rightarrow most work at the root [might expect $O(n^d)$]
3. $RSP > RWS \Rightarrow$ more work each level \Rightarrow most work at the leaves [might expect $O(\# \text{ leaves})$]